Importance of "connectedness" between herds for effective across herd genetic evaluation

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Abstract "Connectedness" is an essential component of genetic evaluations. The degree of connectedness affects the accuracy of comparing estimated breeding values (EBVs) from one herd or contemporary group to the other. It can be measured through Connectedness Rating (CR) which is based on variances and covariance among the estimates of contemporary group effects. A computing algorithm and a computer program for estimating CR is available. The minimum required level of connectedness depends upon the size of the contemporary groups the level of accuracy and the residual variance. About 48% CR is required to detect differences between EBVs that are greater than 20% of the standard deviation in the trait for group sizes of about 100 animals. Higher levels are necessary for smaller group sizes and for more accurate comparisons. Breeders participating in a common genetic evaluation program should therefore exchange their superior genetics and possibly use some common testing facilities for meaningful estimates of breeding values. Maintaining a good connectedness level will make the genetic evaluation program more useful for selection of superior breeding animals and achieving faster rate of genetic progress

Keywords connectedness breeding values genetic evaluation

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1 The concept of connectedness

The term "connectedness" is commonly used in an in albreeding in relation to the genetic evaluations and across herd comparison of estimated breeding values. In this context connect edness is a measure or accuracy of across herd evaluations. It can be described as a measure of the relationships between herds or contemporary groups based on their effect on the accuracy of comparing the genetic values of an in als from one herd or group to the other

In true statistical sense a data set is con-

nected if the difference between effects of every pair of the same fixed factor is estimable in a model of main effects only 1. In genetic evaluation models especially using BLUP, the herds or contemporary groups constitute the pairs of fixed factors and the differences between them need to be estimable in order to compare genetic evaluations of animals from these groups. The accuracy of differences between individuals from these subclasses is affected by the degree of connectedness between subclasses

The accuracy of the estimates of breeding values commonly referred as "repeatability" de-

pends upon heritability of the trait and the a mount of information available for the estimation such as number of records on individual and relatives. It reflects the reliability of the estimated breeding value (EBV) as a guide to the true breeding value. However, it is not necessarily a good indicator of the accuracy of comparing EBVs from one contemporary group to the other. The accuracy of such comparisons depends upon the degree of connectedness between the contemporary groups.

This concept of connectedness applies to con temporary groups within a herd or con temporary groups from different herds Very often there is an interest to know if two herds have suf ficient degree of connectedness between them to include them in a common genetic evaluation program. This is useful in ranking of individuals across herds and in identifying the best individuals for selection and genetic in provement this case each he id may be considered as a sepa rate contemporary group. If there are several con temporary groups within a herd one may select a particular contemporary group to represent the head. For example, if there are several head year season classes within a herd the latest herd year season group may be considered as representative of the herd These contemporary groups are henceforth referred to as herds for simplicity

1. 1 Connectedness as a statistical measure

An illustration of the concept of connectedness in genetic evaluations is given in Fig 1. Herd A and herd B are connected because of the common sine. Sine 1, is used in both herds. Herds B and C are also connected because of the common sine. Sine 2. However, herds C and D are not connected since there is no common genetic link between them. Therefore, differences between EBVs of animals from herd B and C are

estimable and comparable However EBVs of animals from herds C and D can not be compared with sufficient accuracy as the herds are disconnected. In fact it is not always necessar ry to have direct genetic links between herds The connectedness can also occur due to indirect genetic links In this example herds A and C are also connected indirectly through herd B because of Sires 1 and 2. This is true even if the herds contain animals that are not genetically related. For example, if the animals from herd C and herd D are tested in a test station the herds C and D would be connected and that way all the four herds A, B, C and D would be connected It is important to note that connectedness is a statistical measure related to the ability to have estimable comparisons Similar views have been expressed by Kennedy and Trus 21 and Hanocq et a 1³. Genetic links are not absolutely neces sary for connectedness to exist Nevertheless they are important and useful ways of increasing the degree of connectedness

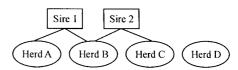


Fig 1 Connectedness among herds through common genetic links

1. 2 Degree of connectedness

In a genetic evaluation model it is possible to introduce estimability of differences between EBVs from different herds by treating the herd effects as random effects rather than as fixed effects. However, the main issue is the accuracy of comparisons even if the differences are estimable. The accuracy of such comparisons is affected by the degree of connectedness between the herds even if the herd effects are treated as random and the differences between them are estimable. Therefore, it is important and useful to

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connectedness and disconnectedness. Herds can be connected and differences between the EBV s can be estimable but if the level of connectedness is low, the accuracy of the comparisons will also be low such that it is not very different from that of completely disconnected herds. In fact in a BLUP genetic evaluation model, connectedness between herds would occur through the genetic relationship matrix, genetic groups and several other fixed or random effects [4-5]. However, it is the degree or magnitude of this connectedness that is important for accuracy of across herd comparisons.

2 M easurement of connectedness

2 1 Prediction error variance of differences between EBV s

The method of estimation depends upon the main objective of the use of the estimate A common objective in an in all breeding is the accuracy of comparing EBVs of animals from different herds or contemporary groups. Therefore logically an ideal measure should be based on the accuracy of EBVs within herds and accuracy of their differences across herds. The accuracy of an individual EBV is often measured as the prediction error variance which is the inverse element of the mixed model equations corresponding to the animal. The accuracy of the difference between EBVs of two individuals can be estimated as the prediction error variance of their difference (PEVD) as

PEVD =
$$Var(\hat{a_i} - \hat{a_j}) = Var(\hat{a_j}) - 2cov(\hat{a_j})$$
.

The average accuracy of differences be tween EBVs of two individuals from different herds would then be the average prediction error variance (PEV) of all pair wise differences be tween individuals from the different herds. However computing this statistic in a large genetic evaluation program would involve several pairs of

an imals between one herd and the other and several possible pairs of herds. This can be extremely time consuming therefore an easier method is required.

2 2 Connectedness Rating(CR)

The EBV of an animal with its own record depends upon the deviation of its performance from the estimate of the contemporary group or herd effect and other factors included in the genetic evaluation model Therefore the PEV of the difference between the EBVs of two animals in different herds or groups can be separated into two components one associated with the animals and their relatives This component depends upon the prediction error variance of each EBV, the degree of relationship between the two ani mals and covariances between animal and herd effects The other component is associated with the herd effects them selves which includes vari ances of the estimates of the head effects and the covariance between them. In calculation of the PEVD of animals in the two herds the component associated with the herd effects remains the same for each comparison while that associated with the animals and their relatives is different for each comparison and tends to cancel out over all comparisons as given in the following equation

$$egin{aligned} ext{VED}_{ij} &= ext{Average[PEV}(\hat{a_{ik}} - \hat{a_{jk'}})] pprox \ &Var(\hat{h_i} - \hat{h_j}) \cong Var(\hat{h_i}) + \ &Var(\hat{h_i}) - 2cov(\hat{h_{ii}}), \end{aligned}$$

As a result the average PEV over all comparisons tends towards the PEV of the difference between estimates of the two herd effects. Therefore the PEV of the difference between the herd effects can be used as a measure of the degree of connectedness between two herds. A simulation study by Kennedy and Trus ² suggested that this can be used as an effective estimate form easuring the degree of connectedness and there was a high correlation (0.995) between average PE-ING House. All rights reserved.

VD and VED. These variances and covariances between estimates of herd effects can be used in the following form as Connectedness Rating to estimate of the degree of connectedness.

$$CR_{ij} = \frac{cov(h_{ij})}{\sqrt{Var(h_i) Var(h_j)}},$$

Where $Var(h_i)$, $Var(h_j)$ and $cov(h_{ij})$ are the variances and covariances of estimates of the respective head effects

Considered in this way, the CR seems $s \dot{m} \dot{\tau}$ lar to a correlation between the estimates of the herd effects however it is quite different from a $s \dot{m} p \, l e$ product moment correlation.

The estimation of CR would also involve computation of variances and covariances of the herd estimates. These require inverse elements of mixed model equations corresponding to the herd effects. It is difficult to obtain a direct inverse of the coefficient matrix of mixed model equations for these specific elements. Hence the following procedure was used. According to the matrix theory, the product of a matrix with its inverse is an identity matrix. This is true for the coefficient matrix (w'w) of mixed model equations as well

$$w'w (w'w)^{-1} = I$$

Therefore

$$w w' (w w)_{i}^{-1} = I_{r}$$

where $\mathbf{w}'\mathbf{w} = \text{coefficient matrix of m ixed model}$ equations $\mathbf{I} = \text{identity matrix}$; $\mathbf{I}_i = \text{a vector of the}$ identity matrix corresponding to contemporary group i (a vector with 1 for the contemporary group and zeros); $(\mathbf{w}'\mathbf{w})_i^{-1} = \text{a vector of inverse elements for the } i^{\text{th}}$ contemporary group

In an iterative procedure for solving the mixed model equations appropriate sets of the vector \mathbf{I}_i can be used to obtain inverse elements for a row or column of the corresponding herd effects of interest Each of these vectors can then be in the form of a block of inverse elements containing variances and covariances at

mong the herds of interest. In fact the method can be used more generally to obtain inverse elements for specific rows without a full direct inverse.

This computing algorithm and the estimate of Connectedness Rating were used for about 100 herds participating in the Canadian Swine Improvement Program for the past seven years. It reflects the breeding and testing procedures used. The CR has been very effective in conveying the level of connectedness to the breeders and taking necessary steps to increase it to a more desired level.

2 3 Add itional methods for estinating connectedness

There are alternative methods for estimating connectedness either considering connectedness as a statistical measure or only as a measure of genetic links Two methods for estimating connectedness were described and compared to the estimate of VED by Laloë et al 6. These methods were the squared correlation between prediction and true differences of genetic values (CD) and a connectedness index (IC) sugges ted by Foulley et al 171 which is based on relative decrease in PEV when fixed effects are known It is suggested that CD combines VED and genetic variability. In this way CD provides a combination of connectedness and genetic variabilities ty. The method can be useful for controlling the genetic variability especially when there is an excessive use of a small group of sires leading to problems of inbreeding etc. However if the pri may objective is to get an estimate of the degree of connectedness and provide information to the herds to take necessary steps to increase the levelof connectedness it might be more useful to have an estimate like CR that would specifically measure the degree of connectedness. The issue of decrease in genetic variability is a common problem in dairy cattle and now in sw ine due to

the use of AI and availability of semen from genetically superior individuals in ternationally. It can be dealt with separately by providing more information on the effective progeny per sine effective population size level of inbreeding etc

In a study of test groups in beef cattle Roso et a [18] used four different methods to estimate the degree of connectedness. The methods used included average prediction error variance of the difference between estimated breeding values (PEVD), variance of estimated differences be tween test group effects (VED), total number of direct genetic links (GLT) [9] and Connectedness Rating (CR). The results show that the average PEVD of each of the test groups with all others could be better predicted on the basis of CR or GLT. In the data set used for test groups in beef cattle the GLT which is based on genet ic links only also gave adequate estimates of connectedness comparable to VED and CR

3 Program for calculating the Connectedness Rating

A program for calculating CR available on CCSI website www. ccsi ca /connectedness This program is based on Animal Breeders Tool Kit (ABTK). The ABTK is a set of programs mainly used for genetics evaluations using BLUP approach These are a group of small programs that can be used for simple operations like ma matrix multiplication and for trix inversion building incidence matrices etc. These programs were originally developed for UNIX and Linux environments They have been now converted in to W indows programs for w ider use $v^{[10]}$. The input to these programs is a coefficient matrix file a file containing row numbers for herd effects and a file containing the head identifications The program outputs inverse of a block of the coefficient matrix and the Connectedness Ratings

for each pair of herd effects

4 Level of connectedness needed for across herd genetic comparisons

Very often the question is what level of cornectedness is required for effective across herd comparisons. In a simplified approach, the magnitude of connectedness required depends upon the magnitude of accuracy desired. This can be determined based on a t test as follows:

$$t_{\alpha} < \frac{d}{\sqrt{\mathrm{VED}(\hat{h_i} - \hat{h_j})}},$$

Where t_{α} = value of the Student t statistic for the desired level of significance α ; d = the average difference between EBVs that needs to be detected VED($h_i^2 - h_j^2$) = variance of estimated difference between herds h_i and h_j .

The relationship between Connectedness Rating and VED can be described as follows according to Mathur et al [11]:

$$VED(\hat{h_i} - \hat{h_j}) = Var(h_i) + Var(h_j) - 2 \omega v(h_{ij}) = Var(h_i) + Var(h_j) - 2 CR_{ij} \sqrt{Var(h_i) Var(h_j)},$$

Hence the level of Connectedness Rating required is

$$\operatorname{CR} > \frac{\left[\operatorname{\textit{Var}}(\hat{h_i}) + \operatorname{\textit{Var}}(\hat{h_j}) \right] - \frac{d^2}{t_{\alpha}^2}}{2 \sqrt{\operatorname{\textit{Var}}(\hat{h_i}) \operatorname{\textit{Var}}(\hat{h_j})}},$$

A rough approximation of the VED $(\hat{h_i} - \hat{h_j})$ based on management group size is

$$VED(\hat{h_i} - \hat{h_j}) \stackrel{\text{def}}{=} \sigma_e^2 \left(\frac{1}{n_i} + \frac{1}{n_j} - 2 \frac{CR_{ij}}{\sqrt{n_i n_j}} \right),$$

Where σ_e^2 = residual variance for the trait and n_i and n_j are the number of records in the management groups or herds

Defined in this way the t statistic required to detect a significant difference d_t at a probatility of t and t are t are t and t are t are t and t are t are t and t are t and

fficient matrix and the Connectedness Ratings bility level \alpha is 21994-2016 China Academic Journal Electronic Publishing Flouse. All rights reserved. http://www.cnki.net

$$t_{\alpha} < \frac{d}{\sqrt{\sigma_{e}^{2}\left[\frac{1}{n_{i}} + \frac{1}{n_{j}} - 2\frac{\operatorname{CR}_{ij}}{\sqrt{n_{i}n_{j}}}\right]}},$$

The required level of connectedness can be obtained by:

$$\operatorname{CR}_{i} > \sqrt{n_{i}n_{j}} \frac{1}{2} \left[\left(\frac{1}{n_{i}} + \frac{1}{n_{i}} \right) - \frac{d^{2}}{\sigma_{e}^{2} t_{i}^{2}} \right],$$

In this way the level of connectedness required depends upon the size of the herds or contemporary groups $(n_i \text{ and } n_j)$, level of significance (α) , the average difference between EBVs that needs to be detected (d), and the residual variance σ_e^2 .

If the herd sizes are equal
$$(n_i = n_j = n)$$
:
$$CR_{ij} > 1 - \frac{n}{f_{\alpha}^2} \left(\frac{d}{\sigma}\right)^2,$$

The required Connectedness Rating is a function of the sample size the level of significance and the difference to be detected expressed as a fraction of the residual standard deviation

Considering a typical situation in pig breeding where the average index is standard ized to a mean of 100 and standard deviation is 25 index points it might be of interest to detect the differences greater than 5 index points i.e. a bout 20% of the standard deviation (SD). Let us further assume that the level of significance required is P < 0.05 and size of the contemporary groups from each of the two herds is 100. Then the level of connectedness should be greater than 48%. The magnitude of Connectedness Rating required depending upon the sample size $(n_i = n_j = n)$ and difference to be detected expressed as percentage of the residual standard deviation assuming P < 0.05 is given in Fig. 2.

For more accurate comparisons where the difference to be detected is very small fraction of the standard deviation of the trait a higher level of connectedness is required. This is particularly the case when the sample size is very small published.

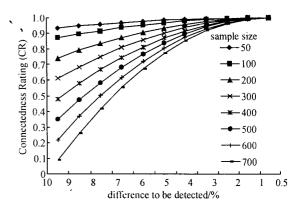


Fig 2 Required levels of Connectedness Rating for different sample size and desired accuracy

A practical way of looking at the desired level of connectedness is examining the existing levels of connectedness between different pairs of herds and their effect on the standard error of difference between estimates of EBVs. The relationship between the Connectedness Ratings of these pairs and the standard error of difference (square root of VED) between the herd effects for the herds in a large population is given in Fig. 3.

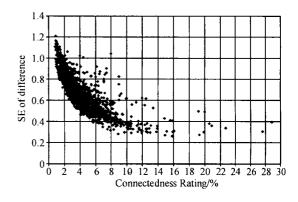


Fig 3 Relationship between standard error (SE) of the difference and Connectedness Rating for litter size

The figure shows a nonlinear relationship between the two variables. The standard error of difference decreases as the Connectedness Rating increases. The Connectedness Rating is very low for many pairs of herds. The error is especially large when connectedness is below 5%.

Therefore his can be considered as the mini

mum level of connectedness required for reasonable across herd comparisons

Connectedness because it is a statistical measure based on the accuracy of the estimates of the herd effects depends on the herd size. The effect of herd size on connectedness is especially large when the size is less than 50 ^[10]. As the sample size increases the level of connectedness depends more on the genetic links rather than the sample size.

5 Recommendations for increasing the level of connectedness

One of the simplest ways to increase connectedness is to use common sizes across herds and contemporary groups. The use of AI boars that have progeny in well connected herds can accelerate the rate of increase in connectedness. It is important to consider the number of progeny the number of herds in which these progeny are found and a weighted connected rating over several herds [11]. U sually about 15% of progeny from well connected sizes in a herd are enough to reach the minimum level of connectedness. One may also use young AI boars that do not have any progeny provided they can e from well connected herds.

The use of central test stations where pigs from several herds are tested under common environmental and management conditions is also a useful way to increase connectedness especially when there are very few genetic exchanges

It is also important to have sufficient size of the contemporary groups in which the EBVs have been calculated. If a contemporary group has less than 10 animals of the same breed, the accuracy of the EBVs is substantially lower. In practical circum stances, it is therefore important to have at least 10 pigs in each contemporary group or head, year season class which is rather a base minimum. These 10 or more pigs should come from at least 3 different sizes to have sufficient connectedness within herds and proper accuracy of the evaluations

In order to have a continuous stream of well connected boars of sufficient genetic merit it is necessary that breeders participating in the program make some of their superior genetics a vailable or form a pool of superior AI boars. This type of participation allows the structure of a national breeding program similar to large nucleus with the possibility of good across herd genetic variability and connectedness. This will allow good across herd comparisons availability of large selection differentials and more genetic progress.

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译文

场间 "关联"在场间遗传评估中的作用

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摘要: "关联"是遗传评估的重要组成部分,关联度影响各场个体或各同期组的估计育种值(EBV s)比较的准确性,可以用关联率(CR)来度量,它是利用同期组效应估计值的方差和协方差来计算的,目前已有相应的算法和计算程序. CR 的最低需要量依赖于同期组的大小、准确性要求和残差方差. 如果对于同期组约有 100 个个体,要检测出的 EB-V s差异大于性状标准差的 20%,则 CR 要达到大约 48%. 如果同期组较小,要求更加准确的比较,则需要更高的 CR. 因此,对于参加同一个遗传评估方案的育种者来说,要进行优秀遗传资源的交换,有可能的话,使用一些共同的测定设备,以使育种值的估计结果有意义. 维持良好的关联水平,可以使选择优秀种猪的遗传评估方案更有价值,获得更快的遗传进展.

关键词: 关联; 育种值; 遗传评估

1 遗传关联的概念

在动物育种中,"关联"的概念主要应用于遗传评估和群间 EBV 的比较. 在这里,关联可以用来度量群间评估的精确性. 在比较不同场或不同群体间个体遗传值估计准确性的影响,"关联"可定义为场间或同期猪群间的相关.

从统计学的角度来看,如果模型里主效应中的每个对应的相同固定效应都可以估计的话,则该数据集是关联的^[1]. 在遗传评估模型,尤其是 BIUP模型中,场效应或同期组效应构成一对固定效应,如果要比较这些组间个体的差异,则场效应或同期组效

应必须是可估的. 次级组间个体差异估计的准确性 受到次级组间关联度的影响.

育种值估计的准确性通常被当作"重复力",它依赖于性状的遗传力,以及评估时可用的信息量,比如个体和亲属记录的数量,它反映了用估计育种值(EBV)对真实育种值进行估计的可靠性,但是它并不能反映不同期组 EBV 比较的精确性,这一准确性依赖于同期组间的关联度.

关联的概念可用于同一场或不同场的同期组个体育种值的比较. 在制订共同的遗传评估计划时, 经常需要知道不同场个体之间的关联是否足够. 它对不同场的个体育种值的排队, 以及在选择和遗传改

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